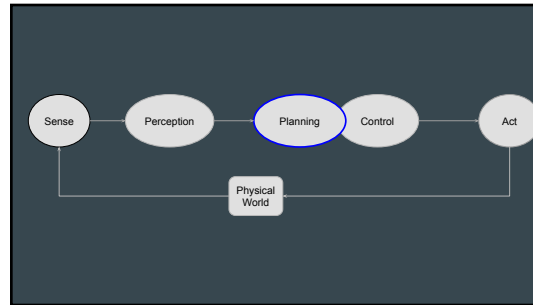


CS4501 Robotics for Soft Eng

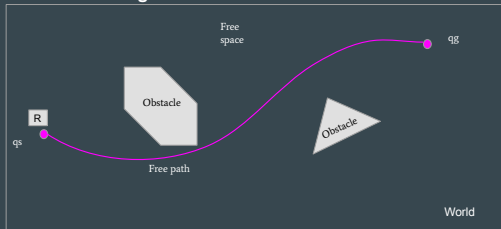
••• Motion Planning



Motion Problem

- Given
 - World Space W
 - Obstacle Regions O
 - Robot State R
 - Starting and Ending Configurations q_s, q_g
- Find a path that modifies R so that
 - From q_s to q_g
 - While staying in W
 - Without hitting any obstacle O
 - [other constraints]

Motion Planning Problem



Motion Planning Families

- Reactive
- Model-based

Work under different assumptions about sensor types and world models available

Motion Planning Families

- Reactive
 - Online
 - Fast, non-optimal

Bug Algorithms



Robot

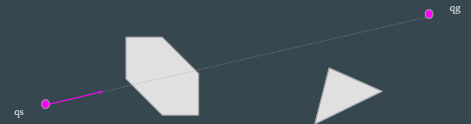
- Is modeled as a bounded point
- Can sense its location precisely
- Can sense contact with obstacles
- Can compute direction towards goal and distance between two points
- Does not know location of obstacles in advanced

Bug Algorithm 1



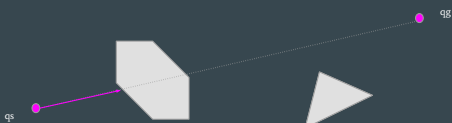
Repeat until Robot-pose = Goal

Bug Algorithm 1



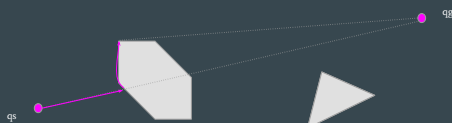
Repeat until Robot-pose = Goal
Head Towards goal

Path Planning Simplified- Bug Algorithm 1



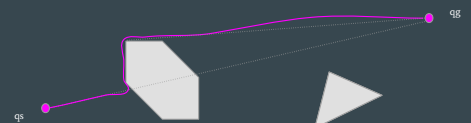
Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall to the left until heading towards goal is possible

Bug Algorithm 1



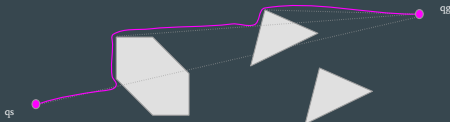
Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall to the left until heading towards goal is possible

Bug Algorithm 1



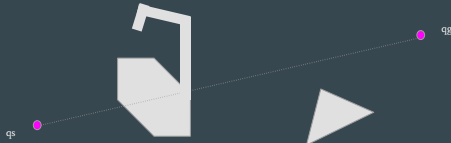
Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall to the left until heading towards goal is possible

Bug Algorithm 1



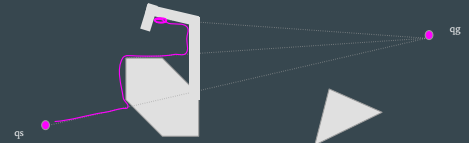
Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall to the left until heading towards goal is possible

Bug Algorithm 1



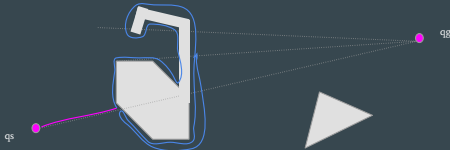
Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall to the left until heading towards goal is possible

Bug Algorithm 1



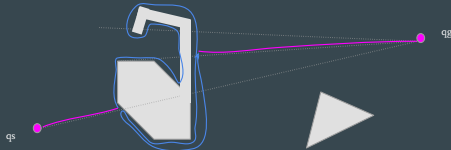
Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall to the left until heading towards goal is possible

Bug Algorithm 1+



Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall completely
Identify closest boundary point to Goal
Return to this point by shortest path along obstacle boundary

Bug Algorithm 1+



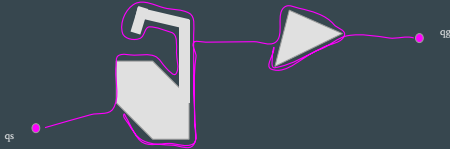
Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall completely
Identify closest boundary point to Goal
Return to this point by shortest path along obstacle boundary

Bug Algorithm 1+ Exercise



Repeat until Robot-pose = Goal
Head towards goal
If obstacle detected then
Navigate next to wall completely
Identify closest boundary point to Goal
Return to this point by shortest path along obstacle boundary

Bug Algorithm 1+ Exercise



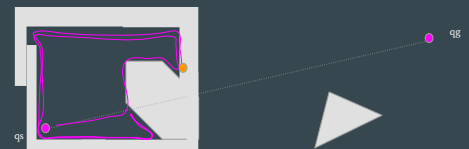
Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Navigate next to wall completely
 Identify closest boundary point to Goal
 Return to this point by shortest path along obstacle boundary

Bug Algorithms 1++



Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Navigate next to wall completely
 Identify closest boundary point to Goal, if direction towards the Goal hits obstacle break
 Return to this point by shortest path along obstacle boundary

Bug Algorithms 1++



Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Navigate next to wall completely
 Identify closest boundary point to Goal, if direction towards the Goal hits obstacle break
 Return to this point by shortest path along obstacle boundary

Bug Algorithm 1++

Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Navigate next to wall completely
 Identify closest boundary point to Goal, if direction towards the Goal hits obstacle break
 Return to this point by shortest path along obstacle boundary

Distance T traveled by Bug-1 (based on D distance between q_s and q_g)

- Lower bound:
- Upper Bound:

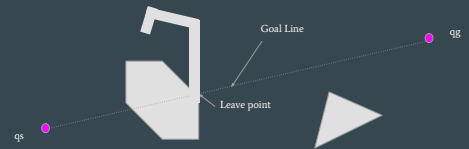
Bug Algorithm 1++

Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Navigate next to wall completely
 Identify closest boundary point to Goal, if direction towards the Goal hits obstacle break
 Return to this point by shortest path along obstacle boundary

Distance T traveled by Bug-1 (based on D distance between q_s and q_g)

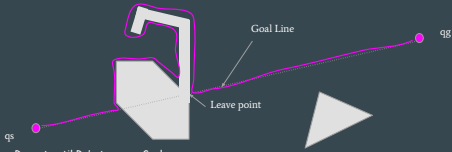
- Lower bound: $T \geq D$
- Upper Bound: $T \leq D + 1.5 \sum(\text{perimeter polygons})$

Bug Algorithm 2



Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Repeat
 Navigate next to wall (to the left)
 Until Goal Line crossed at Leave point closer to goal on the same side than before

Bug Algorithm 2



Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Repeat
 Navigate next to wall (to the left)
 Repeat
 Until Goal Line crossed at Leave point closer to goal on the same side than before

Bug Algorithm 2



Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Repeat
 Navigate next to wall (to the left)
 Repeat
 Until Goal Line crossed at Leave point closer to goal on the same side than before

Bug Algorithm 2 Exercise



Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Repeat
 Navigate next to wall (to the left)
 Repeat
 Until Goal Line crossed at Leave point closer to goal on the same side than before

Path Planning Simplified- Bug Algorithm 2 Exercise



Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Repeat
 Navigate next to wall (to the left)
 Repeat
 Until Goal Line crossed at Leave point closer to goal on the same side than before

Bug Algorithm 2

Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Repeat
 Navigate next to wall (to the left)
 Repeat
 Until Goal Line crossed at Leave point closer to goal on the same side than before

Distance T traveled by Bug-2 (based on D distance between q_s and q_g)

- Lower bound:
- Upper Bound:

Bug Algorithm 2

Repeat until Robot-pose = Goal
 Head towards goal
 If obstacle detected then
 Repeat
 Navigate next to wall (to the left)
 Repeat
 Until Goal Line crossed at Leave point closer to goal on the same side than before

Distance T traveled by Bug-2 (based on D distance between q_s and q_g)

- Lower bound: $T \geq D$
- Upper Bound: $T \leq D + 0.5 \sum (\text{Perimeters of obstacles intersected by goal line} * \text{number of times lines intersects each obstacle})$

Bug Algorithm 2 Exercise

Repeat until Robot-pose = Goal

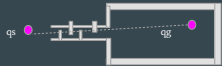
Head towards goal

If obstacle detected then

Repeat

Navigate next to wall (to the left)

Until Goal Line crossed at Leave point closer to goal on the same side than before



Bug Algorithm 2 Exercise

Repeat until Robot-pose = Goal

Head towards goal

If obstacle detected then

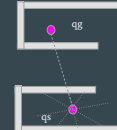
Repeat

Navigate next to wall (to the left)

Until Goal Line crossed at Leave point closer to goal on the same side than before



Relaxing Bug Algorithm assumptions



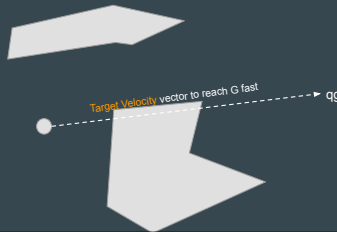
Robot

- Is modeled as a bounded point
- Can sense its location precisely
- Can sense contact with obstacles - can sense more...
- Can compute direction towards goal and distance between two points
- Does not know location of obstacles, has more memory

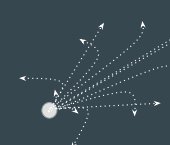
Motion Problem

- Reactive
 - Bug
 - Dynamic windows
- Model-based

Dynamic Windows




Dynamic Windows



For each time slice t
Enumerate allowed velocities in

Dynamic Windows

For each time slice t
Enumerate **allowed** velocities in



Robot Physical Model

Racing drone
Values of the top speeder drone (DJI S900)

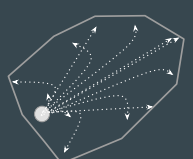
- altitude: only 40 m or 140 ft
- acceleration: from 0 to 100 km/h (vertical) for below 2 s
- duration to reach 100 meters above the ground from the hover: 2.8 s
- maximum acceleration: 3.0 g @ 25 m/s²
- take-off weight: 222 g
- maximum power: 2.250 Watt
- power-to-weight ratio: 2438 W/kg

Dynamic Windows

For each time slice t
For each v in $[\text{curr.v} - \text{maxacc}(t), \text{curr.v} + \text{maxacc}(t)]$

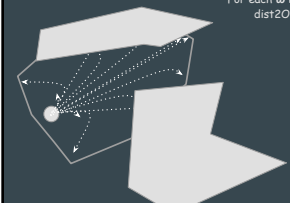
If $(v < \text{maxV}$ and $v > \text{minV})$
validVelocities.add(v)

For each ω in $[\text{curr.}\omega - \text{maxacc}(t), \text{curr.}\omega + \text{maxacc}(t)]$
If $(\omega < \text{max}\omega$ and $\omega > \text{min}\omega)$
validAngVelocities.add(\omega)



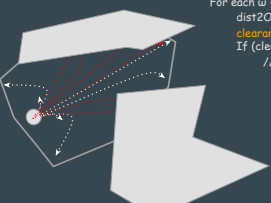
Dynamic Windows

For each v in **validVelocities**
For each ω in **validAngVelocities**
dist2Obstacle = computeDist(v, \omega, laserScan())



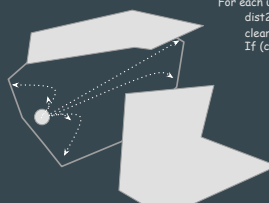
Dynamic Windows

For each v in **validVelocities**
For each ω in **validAngVelocities**
dist2Obstacle = computeDist(v, \omega, laserScan())
clearance = dist2Obstacle - breakDist(v, \omega)
If (clearance > 0)
// non-colliding velocities



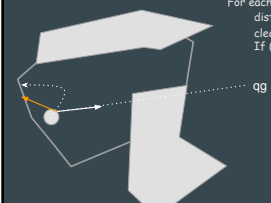
Dynamic Windows

For each v in **validVelocities**
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dist2Obstacle = computeDist(v, \omega, laserScan())
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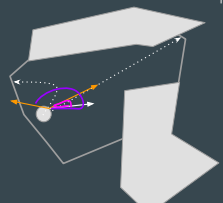


Dynamic Windows

For each v in **validVelocities**
For each ω in **validAngVelocities**
dist2Obstacle = computeDist(v, \omega, laserScan())
clearance = dist2Obstacle - breakDist(v, \omega)
If (clearance > 0)
offHeading = headingDiff(robot.pose, qg, v, \omega)



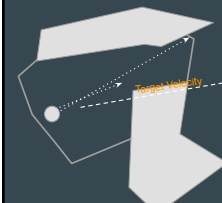
Dynamic Windows



```

For each v in validVelocities
  For each w in validAngVelocities
    dist2Obstacle = computeDist(v, w, laserScan())
    clearance = dist2Obstacle - breakDist(v)
    If (clearance > 0)
      offHeading = headingDiff(robot.pose, qg, v, w)
  
```

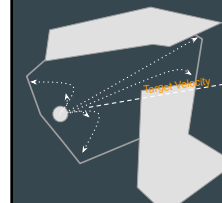
Dynamic Windows



```

For each v in validVelocities
  For each w in validAngVelocities
    dist2Obstacle = computeDist(v, w, laserScan())
    clearance = dist2Obstacle - breakDist(v)
    If (clearance > 0)
      offHeading = headingDiff(robot.pose, qg, v, w)
      offVel = abs(targetVelocity - v)
  
```

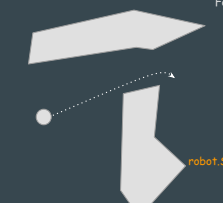
Dynamic Windows



```

For each v in validVelocities
  For each w in validAngVelocities
    dist2Obstacle = computeDist(v, w, laserScan())
    clearance = dist2Obstacle - breakDist(v)
    If (clearance > 0)
      offHeading = headingDiff(robot.pose, qg, v, w)
      offVel = abs(targetVelocity - v)
      output = ka*clearance + kb* offHeading + kc*offVel
  
```

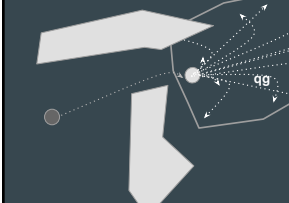
Dynamic Windows



```

For each v in validVelocities
  For each w in validAngVelocities
    dist2Obstacle = computeDist(v, w, laserScan())
    clearance = dist2Obstacle - breakDist(v)
    If (clearance > 0)
      offHeading = headingDiff(robot.pose, qg, v, w)
      offVel = abs(targetVelocity - v)
      output = ka*clearance + kb* offHeading + kc*offVel
      if (output > chosen)
        chosenV = v
        chosenW = w
        chosen = output
  robot.Speed(chosenV, chosenW)
  
```

Dynamic Windows



```

For each v in validVelocities
  For each w in validAngVelocities
    dist2Obstacle = computeDist(v, w, laserScan())
    clearance = dist2Obstacle - breakDist(v)
    If (clearance > 0)
      offHeading = headingDiff(robot.pose, qg, v, w)
      offVel = abs(targetVelocity - v)
      output = ka*clearance + kb* offHeading + kc*offVel
      if (output > chosen)
        chosenV = v
        chosenW = w
        chosen = output
  
```

Dynamic Windows

- Velocity planner (clearance, heading, velocity)
- Considers Robot's Dynamics for valid velocities

Motion Planning Families

- Reactive
- Model-based

Path Planning with Models

- Reactive
- Model-based
 - Predictive model of robot actions in **known** world
 - Build simplified representation
 - Search for solution in world representation

Path Planning: Visibility Methods



Assumptions

- Robot modeled as a bounded point
- Can sense its location precisely
- Can compute direction towards goal and distance between two points
- Knows location of obstacles in advance - **polygonal obstacles**

Path Planning: Visibility Methods



- Assumption: known polygonal obstacles

Path Planning: Visibility Methods



- Assumption: known polygonal obstacles
- Connect all vertices without obstacles in between

Path Planning: Visibility Methods



- Assumption: known polygonal obstacles
- Connect all vertices without obstacles in between
- Graph search!

Path Planning: Visibility Methods



- Assumption: known polygonal obstacles
- Connect all vertices without obstacles in between
- Graph search algorithm

Path Planning: Visibility Methods



When does it fail?

Path Planning with Models

- Reactive
- Model-based
 - Visibility
 - Grid

Path Planning: Grid Methods



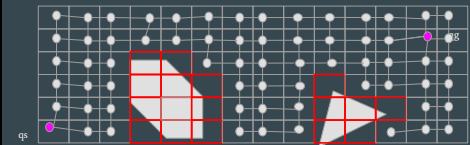
- Discretization of space - resolution

Path Planning: Grid Methods



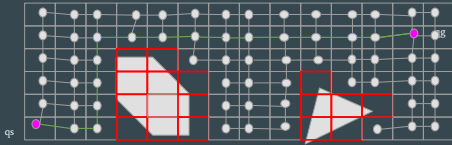
- Discretization of space
- Occupancy checker - probability

Path Planning: Grid Methods



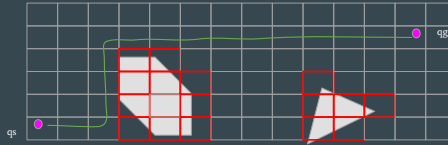
- Discretization of space
- Occupancy checker - probability

Path Planning: Grid Methods



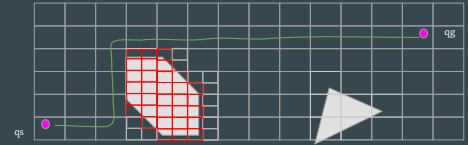
- Discretization of space
- Occupancy checker
- Graph search algorithm on free cells

Path Planning: Grid Methods



- Discretization of space
- Occupancy checker
- Graph search algorithm on free cells
- Dependent on cell dimensions
- Subject to shape of objects

Path Planning: Grid Methods with Refinement

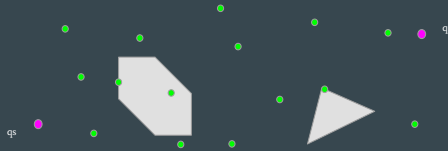


- Discretization of space
- Occupancy checker
- Graph search algorithm on free cells
- Dependent on cell dimensions
- Subject to shape of objects

Path Planning with Models

- Reactive
- Model-based
 - Visibility
 - Grid
 - Probabilistic

Path Planning: Probabilistic Roadmap



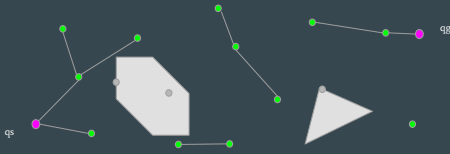
- Random sample of points in space

Path Planning: Probabilistic Roadmap



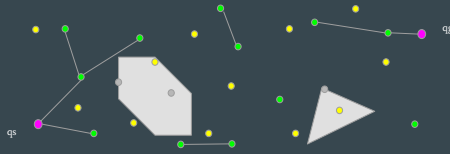
- Random sample of points in space
- Drop samples over obstacles

Path Planning: Probabilistic Roadmap



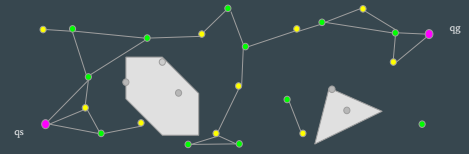
- Random sample of points in space
- Drop samples over obstacles
- Connect samples to k-nearest neighbors

Path Planning: Probabilistic Roadmap



- Random sample of points in space
- Drop samples over obstacles
- Connect samples to k-nearest neighbors
- Sample more points until q_s and q_g are connected

Path Planning: Probabilistic Roadmap



- Random sample of points in space
- Drop samples over obstacles
- Connect samples to k-nearest neighbors
- Sample more points until q_s and q_g are connected

Path Planning: Probabilistic Roadmap



- Random sample of points in space
- Drop samples over obstacles
- Connect samples to k-nearest neighbors
- Sample more points until q_s and q_g are connected

Searching in a Graph

- Generic
 - BFS (Breath First)
 - DFS (Depth First)
- Informed
 - "Heuristic" to guide the search

Take Away

- Families of approaches to navigate world
 - Reactive
 - Local area and fast response
 - Model-based
 - Big picture and long paths
 - Build and searching graphs